

Asymptotes

Simplified Method

1. Find horizontal asymptote lines. (see below)
2. Find vertical asymptote lines. (see below)
3. Draw the lines (dotted)
4. For each sector bounded by **vertical asymptote lines**, pick an x and plot the point.
5. Draw Curving line to the asymptotes from each special x

Note: Plotting extra points can help guide you .

General Method

1. **Horizontal Asymptotes** for $R(x) = \frac{P(x)}{Q(x)}$, $P(x)$ and $Q(x)$ polynomials.

A. Only the leading coefficients of P and Q matter. So decide for $\frac{ax^m}{bx^n}$

B. If $m > n$, there is no asymptote.

If $m = n$, $y = \frac{a}{b}$ is the asymptote. Let $c < d$ be x values past all roots of $Q(x)$.

Find $R(c)$ and $R(d)$ to decide if approach is from above or below.

If $m < n$, $y = 0$ is the asymptote. Let $c < 0$ and $d > 0$, $|c|$ and $|d|$ *very large*.

Find $R(c)$ and $R(d)$ to decide if approach is from above or below.

Note: c and d stand for $-\infty$ and ∞ .

2. **Vertical Asymptotes** are where $f(x) = -\infty$ or ∞ .

To find the Vertical Asymptotes for $f(x) = \frac{g(x)}{Q(x)}$, $Q(x)$ polynomial.

Find **All** roots of $Q(x)$, a, b, c, ... Each of $x=a$, $x=b$... is an asymptote..

Find $f(a+)$ and $f(a-)$ to decide if $\rightarrow -\infty$ or ∞ on each side of a. Likewise for b, etc

Solving Inequalities Rename so $a < b$ ($-b < -a$)

1. Solve $(x+a)(x+b) < 0$. Answer: $-b < x < -a$.
2. Solve $(x+a)(x+b) > 0$. Answer: $x < -b$ **OR** $x > -a$.

Solving Absolute value Inequalities

3. $|x-a| < r$ means : $a-r < x < a+r$.
4. $|x+a| < r$ means : $-a-r < x < -a+r$.
5. $|x-a| > r$ means : $x < a-r$ **OR** $x > a+r$

Intercepts

1. y-intercept. Set $x = 0$ and solve for y ($y=c$). y-intercept is (0,c).
2. x-intercept. Set $y = 0$ and solve for x ($x=k$). x-intercept is (k,0).